

5     **METHOD FOR GENERATING A DESIRED STATE OF A PSEUDORANDOM  
SEQUENCE AND A RADIO USING SAME**

**Technical Field**

- 10    This invention relates generally to pseudorandom sequences and more particularly to generating a particular state of a pseudorandom sequence as well as application in a radio.

**Background**

- 15    Pseudorandom sequences are known in the art. Pseudorandom number sequences, for example, are frequently used in encryption applications and are also finding increasing applications in wireless communications. For example, in code division multiple access communication systems, the
- 20    digitized data stream will be spreaded with pseudorandom number codes before transmission. The receiver can despread the digital data stream by applying the same pseudorandom number code as used by the transmitter. To facilitate this, however, the transmitter and receiver must be synchronized with respect to the pseudorandom number sequence. Achieving such
- 25    synchronization can be particularly challenging when a mobile communications unit shifts from a first base station to a second base station. Although the base stations of a given communications system will typically use the same pseudorandom number sequence, this sequence will be offset in time from one base station to another. Therefore, when switching to a new
- 30    base station, a mobile communications unit must newly establish synchronization of the pseudorandom number sequence.

In such a communications system, the generator of a pseudorandom number sequence can have, for example, 15 digits. The number of possible states that such a sequence can attain is  $2^{N-1}$ , where N equals the number of digits in the sequence generator. Therefore, in such a system, there are 32,767 possible states. Adjacent base stations are often offset by a known number of subsequent states from one another. When switching to any given base station, therefore, the mobile communications unit need not attempt all 32,767 possible states to locate the desired state by trial and error. Nevertheless, even though the state offset is likely known, the corresponding phase of the pseudorandom number sequence must still be ascertained.

Each state of the pseudorandom number sequence can be calculated by a corresponding pseudorandom sequence generating polynomial (also often referred to as a mask). Some prior art solutions simply propose storing in memory the specific mask for each possible state of a given pseudorandom number sequence. As depicted in FIG. 1, this approach will result in a mask 1 being stored to calculate a corresponding state S1, a mask 2 being stored to calculate a corresponding state S2, and so forth. When the number of states is relatively large, this can require unfeasible amounts of memory (especially for a portable communications device).

Another prior art approach is depicted in FIG. 2. In this approach, not every potential state has a corresponding mask stored for it. Instead, masks for corresponding states are equally distributed throughout the sequence of potential states. For example, when working with a number like 32,767, a not uncommon spacing would be 64 states. Therefore, as depicted, a mask 2 would be provided to derive state S64 and another mask 3 would be provided 64 spaces later to derive state S128 (and so forth throughout the sequence). This approach allows calculation of a state that is within 32 states of any target state within the sequence. A next-state mask (in the example shown this would be mask 1) could then be utilized to incrementally calculate each

succeeding next state until the target state has been reached. While this approach has significantly reduced memory requirements (only 513 masks need be stored as versus 32,767), significant processing time is potentially required. This calculation time can be critical, and particularly when seeking to  
5 synchronize to a moving target as exists in a communications system as referenced above.

A need therefore exists for a way to relatively quickly and reliably move from a first state of a pseudorandom sequence to a second potentially arbitrary state  
10 without requiring undue dedicated memory and while minimizing processing requirements. Preferably, the solution should be amenable to implementation in either a hardware based or software based embodiment.

### **Brief Description of the Drawings**

15 These needs and others are substantially met through provision of the method for calculating a desired state of a pseudorandom sequence as disclosed below. These benefits and others will become more clear upon making a thorough review and study of the following detailed description, particularly  
20 when studied in conjunction with the drawings, wherein:

FIG. 1 comprises a prior art depiction of a first mask storage scheme;

FIG. 2 comprises a prior art depiction of a second mask storage scheme;

25 FIG. 3 comprises a flow diagram configured in accordance with various embodiments of the invention;

FIG. 4 comprises a detailed flow diagram configured in accordance with  
30 various embodiments of the invention;

FIG. 5 comprises a diagrammatic depiction of one embodiment of a mask storage scheme configured in accordance with the invention;

FIG. 6 comprises a diagrammatic depiction of mask derivation in accordance with various embodiments of the invention;

FIG. 7 comprises a schematic representation of mask calculation using multiple mask extrapolation in accordance with various embodiments of the invention; and

FIG. 8 comprises a system level diagrammatic depiction of a radio communications system having a radio configured in accordance with various embodiments of the invention.

## Detailed Description

Pursuant to the various embodiments presented below, only a few masks comprising pseudorandom sequence generating polynomials need be initially stored in order to permit rapid and efficient derivation of any given mask as required to calculate any given pseudorandom sequence state (as will be shown below, if desired only one initial mask need be originally stored). These various embodiments utilize one or more existing masks to generate a new mask that is capable of calculating a state that is closer (or equal) to the target state than any of the existing masks. This process can be iterated to move progressively closer to the target state as required. Though the masks can be equally distributed across the potential states as is done in some prior art approaches, in fact superior performance should ordinarily be expected by an unequal distribution. As will be seen below, in one embodiment a more or less logarithmic distribution provides satisfactory performance.

As a result, memory requirements are dramatically minimized while computational requirements are either no worse or often favorably impacted.

Referring now to FIG. 3, an overall description of basic activities in

5 accordance with various embodiments of the invention will now be described. To begin, a starting state for a pseudorandom sequence of the items (wherein the items can be numbers such as binary 1's and 0's), wherein the pseudorandom sequence of items has a corresponding finite number of potential states (for purposes of this description, the pseudorandom sequence  
10 of items will be presumed to have 32,767 potential states though it should be understood that the invention has application for any number of finite potential states) is provided 31. For example, within the context of a wireless communications system, the starting state would likely be the present state of the pseudorandom sequence.

15 A next-state mask is also provided 32. The next-state mask comprises a pseudorandom sequence generating polynomial that determines the next state of the pseudorandom sequence. For example, if the present state is state X (where X simply represents any given state within the finite number of potential states for the pseudorandom sequence), the next-state mask will  
20 calculate state X+1. Such next-state masks are well understood and commonly used in the prior art. This particular mask has importance in part because the shift to a next adjacent subsequent state comprises the finest resolution move that is possible.

25 The target state (that is, the subsequent state of the pseudorandom sequence that is presently desired) must be identified 33. In many applications, this simply requires adding a known offset to the starting state. For example, if the present state is state X and if the known offset is 64 then the target state  
30 would be state X+64. More particularly, this target state represents the state of the pseudorandom sequence after the next-state mask has been iterated

64 times. Again, however, one benefit of these embodiments is that such a target state can be achieved without requiring 64 successive iterations.

Other masks in addition to the next-state mask can be provided 34 as well. It should be understood that the target state could be attained even though only the next-state mask were initially provided, and therefore the provision 34 of an additional mask or masks is optional. For most applications, however, providing additional masks will significantly reduce the time required to resolve to the target state. Importantly, the number of additional masks need not be large. For example, if the pseudorandom sequence has 32,767 potential states, 5 to 15 additional masks will readily facilitate the process (particularly if selected appropriately). The additional masks can be selected with corresponding relative state locations positioned anywhere within the finite number of potential states for the pseudorandom sequence. The additional masks can be selected, for example, to correspond to state locations that are evenly spaced throughout the potential states. Preferably, however, the additional masks are distributed more unevenly throughout the finite number of potential states for the pseudorandom sequence. Additional explanation and illustrations will be provided below regarding selection of specific additional masks.

With knowledge of the starting state and the target state, and with at least one initially provided mask, a mask(target) that will correspond to the target state is derived 35 (or identified if the necessary polynomial turns out to already be available). The mask(target) is derived 35 by combining other masks (when only one mask is available, then that mask can be combined with itself). By using this approach (which will typically require more than one iteration as will be shown below) any mask as will derive any state within the finite number of potential states for the pseudorandom sequence can be derived. By appropriate selection of the initial masks, relatively quick resolution with relatively few iterations can be ordinarily expected.

Once the mask(target) has been derived 35 (or again, identified if it already exists and does not need derivation) it can be used 36 to calculate the desired target state. By needing only a few originally provided masks to efficiently work a relatively large number of potential states, the memory requirements to support this process are greatly reduced as compared to prior art approaches. Furthermore, the number of iterations required to reach the mask(target) are not unduly large as compared to prior art approaches, and with appropriately selected initial masks can actually be less than competing solutions.

- Referring now to FIG. 4, additional details regarding various embodiments to support this process will be described. As related above, a starting state is provided 31 and a target state is identified 33. The masks are then provided 34. As noted above, a single mask can be provided if desired (when only using a single mask, the next-state mask is a natural choice; nevertheless, other masks could be utilized as well). More typically, however, multiple masks are provided 34. As noted above, these masks are preferably unevenly distributed with respect to the potential states. With momentary reference to FIG. 5, the masks can correspond to states in a way that approximates or equals a logarithmic distribution. Accordingly, as depicted in FIG. 5 (which illustrates general relationships but is not drawn to scale), the space between state SA and state SB (and hence the number of states between state SA and state SB) is smaller than the space between state SB and state SC. In a similar fashion, the number of states separating subsequent selected states (such as state SD and state SE) increases as well. A preferred, but not required approach, is to space at least the wider gaps as an approximation of a logarithmic distribution (states associated with smaller gaps tend to be less useful and hence strict observation of a logarithmic distribution for smaller values can often be dispensed with without undue degradation of performance). By providing masks that will derive these selected states (such as mask A to derive state SA and mask E to derive state SE) a highly usable group of masks can be provided 34. Again, 5 to 15 well chosen masks will

readily suffice to facilitate resolving towards any specific state within a sequence having 32,767 potential states.

As generally described with reference to FIG. 3, the provided mask or masks are utilized to derive the required mask(target). Usually, it will be unlikely that the mask(target) can be derived in a single iteration. The likelihood of being able to achieve a single iteration success will increase as the number of available masks increases. Since this process can resolve relatively quickly when using only a few masks, however, greatly increasing the number of available masks in order to more likely ensure a single iteration derivation will usually not provide any significant advantage. Therefore, multiple iterations are likely.

The available masks are therefore utilized to derive a new mask having a corresponding state that is relatively closer to the target state. Preferably, the masks are utilized in a way to allow derivation of a new mask or selection of an existing mask that will represent a corresponding state that is closest to the target state.

Once a mask has been derived or otherwise selected, the process can determine whether the resultant mask in fact represents the mask(target). If true, the corresponding state can be calculated and the process concluded. If the resultant mask comprises an interim mask but does not represent the mask(target), the process can determine whether one or more next-state executions will suffice to calculate the target state. If true, the next-state polynomial can be utilized to close a small remaining gap. Optionally, the process can also determine whether slewing should be utilized to achieve the desired target state (slewing is a well understood process whereby two slightly unsynchronized pseudorandom sequences can be brought into synchronicity). If appropriate, slewing can be utilized to calculate the target state. Otherwise, the process will iterate and once



again utilize the masks to derive a new mask (each successive iteration can also utilize earlier derived masks in addition to the originally provided masks, thereby providing increasing variety and opportunity for rapid closure).

- 5 FIG. 6 may help illustrate the combining of masks to derive a new mask. All possible states for a given pseudorandom sequence are illustrated as existing between an original state SO and a last state SN. A first mask MASK 1 comprises a next-state mask and therefore represents movement to a next state (in this example, state S1). MASK 2 will calculate a state S2 that is  
10 greatly removed from the original state. MASK 3 represents a mask that would result by combining MASK 1 with a MASK 2. MASK 4 represents a mask that would result by combining MASK 3 with itself (note that upon reaching the last state SN the series of states simply begin again with the initial state SO), which new mask will calculate a corresponding state S4.

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It can therefore be seen that one or more masks can be combined with themselves or other masks to thereby derive new masks. These new masks can be utilized to calculate corresponding new states of the pseudorandom sequence.

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A very common way to represent a unique pseudorandom number sequence generator is to use the generation polynomial:

$$f(x) = x^N + g_{N-1}x^{N-1} + g_{N-2}x^{N-2} + \dots + g_1x + 1 \quad (1)$$

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An equivalent linear recursive representation (sometimes known as a Fibonacci representation) can be written as:

$$i(n+N) = \sum_{k=0}^{N-1} g_k i(n+k) = \vec{G} \bullet \vec{I}_n \quad (2)$$

Where  $\vec{G} = \{g_{N-1}, g_{N-2}, \dots, g_1, g_0\}$ ,  $\vec{I}_n = \{i(n+N-1), i(n+N-2), \dots, i(n+1), i(n)\}$  and  $\bullet$

- 5 stands for inner product operation between two vectors. The secondary output of the pseudo random number sequence generator, with an arbitrary P-chip (also often referred to as bit or state) ( $P > N$ ) offset, can be generated using the shift-and-add property of pseudo random number sequence, i.e.:

$$i(n+p) = \sum_{k=0}^{N-1} p_k i(n+k) = \vec{M}_p \bullet \vec{I}_n \quad (3)$$

Where the offset p is referenced to the output state  $i(n)$ . This denotes  $\{g_{N-1}, g_{N-2}, \dots, g_1, g_0\}$  as a mask vector  $\vec{M}_p$  constructed by  $p_k (k=0, \dots, N-1)$  from the above equation. (Computing these elements of a mask vector for an arbitrary  
15 offset is helpful for facilitating synchronization by a spread spectrum receiver.)

Similarly, by replacing p with p+1, one determines:

$$\begin{aligned} i(n+p+1) &= \sum_{k=0}^{N-1} p_k i(n+k+1) = p_{N-1} i(n+N) + \sum_{k=0}^{N-2} p_k i(n+k+1) \\ &= p_{N-1} \sum_{k=0}^{N-1} g_k i(n+k) + \sum_{k=1}^{N-1} p_{k-1} i(n+k) \\ &= \sum_{k=1}^{N-1} (p_{N-1} \cdot g_k + p_{k-1}) \cdot i(n+k) + p_{N-1} \cdot g_0 \cdot i(0) \\ &= \vec{M}_{p+1} \bullet \vec{I}_n \end{aligned} \quad (4)$$

We can calculate  $\vec{M}_{p+1}$  through the following equation:

$$\vec{M}_{p+1} = (\vec{M}_p \ll 1) + p_{N-1} \cdot \vec{G} \quad (5)$$

The above approach constitutes a single extrapolation mechanism as often appears in prior art technique. It is this mechanism that allows calculation of a mask that derives a state with one extra offset.

Now, let's replace p with another offset q. Using a similar Fibonacci representation as before, this yields:

$$i(n+q) = \vec{M}_q \bullet \vec{I}_n = \sum_{k=0}^{N-1} q_k i(n+k) \quad (6)$$

Now let  $r=p+q$ .  $i(n+r)$  can be derived from:

$$\begin{aligned} i(n+p+q) &= \sum_{k=0}^{N-1} q_k i(n+p+k) \\ &= \sum_{k=0}^{N-1} q_k \cdot (\vec{M}_{p+k} \bullet \vec{I}_n) \\ &\Rightarrow \vec{M}_{p+q} = \sum_{k=0}^{N-1} q_k \cdot \vec{M}_{p+k} \end{aligned} \quad (7)$$

Where  $\vec{M}_{p+q}$  constitutes mask vectors with offsets p+1, p+2, ..., p+N-1 respectively and can be easily calculated via the single extrapolation method described above.

It has been shown that mask vector  $\vec{M}_{p+q}$  is a linear combination of mask vectors  $\vec{M}_p, \vec{M}_{p+1}, \dots, \vec{M}_{p+N-1}$  and the combining weights are determined by the elements of mask vector  $\vec{M}_q$ . FIG. 7 comprises a logical circuit depiction by which the next-state mask (mask 1) is used to combine two other masks (mask 2 and mask 3) to derive a new mask, the defining elements of which

will appear in the open squares presented in the illustration. These processes are also readily implementable in a programmable computational platform such as a microprocessor.

5 These embodiments allow a relatively few pseudorandom sequence generating polynomials to be utilized to derive other such polynomials to thereby allow calculation of any state within a finite number of potential states for a given pseudorandom sequence of items. Memory requirements are therefore modest. Appropriate selection of these few polynomials can also  
10 result in minimized computational iterations and timely acquisition of the desired state. The process is readily implementable in hardware and yet is highly suitable for software implementations as well. As a result, various implementation platforms can be utilized to attain the benefits of these embodiments.

15 For example, referring to FIG. 8, a wireless communications system 80, such as a code division multiple access system, can have a first base station 81 transmitting code division multiple access radio frequency signals 82 that use a specific phase of a specific pseudorandom sequence of numbers for  
20 synchronization purposes and a second base station 83 that transmits code division multiple access radio frequency signals 84 that use a different phase of the same specific pseudorandom sequence of numbers, all in accordance with well understood prior art technique. A radio 85 that is compatibly receiving wireless signals 82 from the first base station 81 will not  
25 automatically be able to receive wireless signals 83 from the second base station 84 upon traveling within range of the second base station 83 because the synchronization pseudorandom sequence will be out of phase with the radio's 85 present settings.

30 By using the known offset between states of the pseudorandom sequence of numbers, however, the radio 85 can utilize any of the embodiments taught

above to quickly adjust itself to the correct phase of the sequence for the second base station 83 and begin receiving signals 84 from that source. This capability can of course be rendered in hardware, software, or a combined hardware/software in the radio 85 as appropriate to the capabilities of the  
5 radio, the radio's form factor requirements, power usage limitations, and so forth.

Those skilled in the art will recognize that yet further modifications, alterations, and combinations can be made with respect to the various embodiments set  
10 forth. Such modifications, alterations, and combinations should be viewed as within the contents of these teachings and are within the spirit and scope of the invention.

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